

# Approximating fixed points of asymptotically demicontractive mappings by iterative schemes defined as admissible perturbations

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## ABSTRACT.

We establish convergence theorems for a Krasnoselskij type fixed point iterative method constructed as the admissible perturbation of an asymptotically demicontractive operator defined on a convex closed subset of a Hilbert space.

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