CARPATHIAN J. MATH. Online version available at http://carpathian.ubm.ro
34 (2018), No. 1, 93 - 102 Print Edition: ISSN 1584 - 2851 Online Edition: ISSN 1843 - 4401

Suzuki ψF-contractions and some fixed point results

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ABSTRACT.

The purpose of this paper is to combine and extend some recent fixed point results of Suzuki, T., [*A new type of fixed point theorem in metric spaces*, Nonlinear Anal., **71** (2009), 5313–5317] and Secelean, N. A. & Wardowski, D., [*ψF-contractions: not necessarily nonexpansive Picard operators*, Results Math., **70** (2016), 415–431]. The continuity and the completeness conditions are replaced by orbitally continuity and orbitally completeness respectively. It is given an illustrative example of a Picard operator on a non complete metric space which is neither nonexpansive nor expansive and has a unique continuity point.

Acknowledgements. Project financed by Lucian Blaga University of Sibiu research grants LBUS-IRG-2017-03.

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Received: 16.10.2016; In revised form: 08.06.2017; Accepted: 15.06.2017
2010 *Mathematics Subject Classification.* 47H09, 47H10, 45D05.
Key words and phrases. *ψF-contraction, F-contraction, nonexpansive, expansive, fixed point, Picard operator, Suzuki contraction.*

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