

A new class of metric f -manifolds

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ABSTRACT.

We introduce a new general class of metric f -manifolds which we call (almost) trans- S -manifolds and includes S -manifolds, C -manifolds, s -th Sasakian manifolds and generalized Kenmotsu manifolds studied previously. We prove their main properties and we present many examples which justify their study.

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