Fixed point theorems for contractions in semicomplete semimetric spaces

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Abstract. We introduce the concept of semicompleteness on semimetric space, which is weaker than completeness. We prove fixed point theorems for contractions in semicomplete semimetric spaces. Also, we generalize Jachymski-Matkowski-Świątkowski’s fixed point theorem in semimetric spaces.

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References


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