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Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Fixed point problems concerning contractive type operators on KST-Spaces

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ABSTRACT.

In this paper, using the concept of w-distance we prove some results on the existence of fixed points for contractive type operators, namely; (α, μ)-ψ-contractive operators. Applications are also presented. Our results improve and generalize a number of known results of fixed point theory including the recent results of Guran and Bota [Guran, L. and Bota, M.-F., *Ulam-Hyers Stability Problems for Fixed Point Theorems concerning α-ψ-Type Contractive Operators on KST-Spaces*, Submitted in press.] and Ansari [Ansari, A. H. and Shukla, S., *Some fixed point theorems for ordered F-$(\mathcal{F}, h)$-contraction and subcontractions in θ-f-orbitally complete partial metric spaces*, J. Adv. Math. Stud., **9** (2016), No. 1, 37–53].

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