

Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Convergence of inexact orbits of monotone nonexpansive mappings

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ABSTRACT.

We study monotone nonexpansive self-mappings of a closed and convex cone in an ordered Banach space with particular emphasis on the asymptotic behavior of their inexact iterates.

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