

Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Global Minimization of best proximity points for semi-cyclic Berinde contractions

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ABSTRACT.

In this paper, we introduce a semi-cyclic Berinde contraction pair on a metric space which is more general than that of semi-cyclic contraction pair defined by Gabeleh and Abkar [Gabeleh, M. and Abkar, A., *Best proximity points for semi-cyclic contractive pairs in Banach spaces*, Int. Math. Forum, **6** (2011), 2179–2186] and prove an existence result concerning global monomization of best proximity points of this pair. Our main result can be used to obtain a common fixed point theorem of some contractive mappings related to Berinde's contractions without commutative assumption. An example supporting our main result is also given.

Acknowledgement. This reserach was supported by Chiang Mai University.

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Received: 20.09.2017; In revised form: 17.01.2018; Accepted: 15.07.2018

2010 Mathematics Subject Classification. 41A65, 41A52.

Key words and phrases. *best proximity point, semi-cyclic contraction, berinde semi-cyclic contraction.*

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