

Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Improvements on Bogin-type fixed point theorems in complete metric spaces

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ABSTRACT.

We improve Bogin-type fixed point theorems in complete metric spaces. We also compare these theorems with a Ćirić-type fixed point theorem and others.

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