

Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Fixed point results of generalized almost G - contractions in metric spaces endowed with graphs

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ABSTRACT.

The main aim of this paper is to introduce a class of generalized contractions in the sense of Berinde. Some examples and fixed point theorems for such introduced mappings in the setting of metric spaces endowed with a graph are discussed. Our results extend and include many existing results in the literature.

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