

Dedicated to Professor Yeol Je Cho on the occasion of his retirement

Iterative algorithms for split common fixed points of demicontractive operators without priori knowledge of operator norms

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ABSTRACT.

The split common fixed points problem for demicontractive operators has been studied in Hilbert spaces. An iterative algorithm is considered and the weak convergence result is given under some mild assumptions.

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