

Best Ulam constant for a linear difference equation

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ABSTRACT.

In this paper we provide some results on Ulam stability for the linear difference equation of order one in Banach spaces and we determine its best Ulam constant. The main result is applied to a process of loan amortization.

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