Coincidence point theorems for cyclic multi-valued and hybrid contractive mappings

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ABSTRACT.

In this paper, we consider the existence theorem of coincidence point for a pair of single-valued and multi-valued mapping that are concerned with the concepts of cyclic contraction type mapping. Some illustrative examples and remarks are also discussed.

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