

Dedicated to Prof. Juan Nieto on the occasion of his 60<sup>th</sup> anniversary

## A generalization of the Pompeiu mean-value theorem to compact sets

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### ABSTRACT.

We generalize the Pompeiu mean-value theorem by replacing the graph of a continuous function with a compact set.

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