

Dedicated to Prof. Juan Nieto on the occasion of his 60th anniversary

Ulam-Hyers-Rassias stability of some quasilinear partial differential equations of first order

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ABSTRACT.

In this paper we investigate the Ulam-Hyers-Rassias stability for some quasilinear partial differential equations.

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