

Dedicated to Prof. Qamrul Hasan Ansari on the occasion of his 60th anniversary

A cyclic coordinate-update fixed point algorithm

BO PENG and HONG-KUN XU

ABSTRACT.

We prove that a cyclic coordinate fixed point algorithm for nonexpansive mappings when the underlying Hilbert space is decomposed into a Cartesian product of finitely many block spaces is weakly convergent to a fixed point of the mapping under investigation. Our result relaxes a condition imposed on the stepsizes of Theorem 3.4 of Chow, et al [Chow, Y. T., Wu, T. and Yin, W., *Cyclic coordinate-update algorithms for fixed-point problems: analysis and applications*, SIAM J. Sci. Comput., **39** (2017), No. 4, A1280–A1300].

REFERENCES

- [1] Chow, Y. T., Wu, T. and Yin, W., *Cyclic coordinate-update algorithms for fixed-point problems: analysis and applications*, SIAM J. Sci. Comput., **39** (2017), No. 4, A1280–A1300
- [2] Geobel, K. and Kirk, W. A., *Topics in Metric Fixed Point Theory*, Cambridge Studies in Advanced Mathematics, **28**, Cambridge University Press, 1990
- [3] He, H. and Xu, H. K., *Perturbation resilience and superiorization methodology of averaged mappings*, Inverse Problems, **33** (2017), No. 4, 044007, 11 pp.
- [4] Krasnoselskii, M. A., *Two remarks on the method of successive approximations*, Uspehi Math. Nauk., **10** (1955), 123–127 (in Russian)
- [5] Lopez Acedo, G. and Xu, H. K., *Iterative methods for strict pseudo-contractions in Hilbert spaces*, Nonlinear Anal., **67** (2007), 2258–2271
- [6] Mann, W. R., *Mean value methods in iteration*, Proc. Amer. Math. Soc., **4** (1953), 506–510
- [7] Nedic, A. and Bertsekas, D. P., *Incremental subgradient methods for nondifferentiable optimization*, SIAM J. Optim., **12** (2001), No. 1, 109–138
- [8] O'Hara, J. G., Pillay, P. and Xu, H. K., *Iterative approaches to convex feasibility problems in Banach spaces*, Nonlinear Anal., **64** (2006), 2022–2042
- [9] Opial, Z., *Weak convergence of the sequence of successive approximations of nonexpansive mappings*, Bull. Amer. Math. Soc., **73** (1967), 595–597
- [10] Peng, Z., Xu, Y., Yan, M. and Yin, W., *Arock: An algorithmic framework for asynchronous parallel coordinate updates*, SIAM J. Sci. Comput., **38** (2016), A2851–A2879
- [11] Polyak, B. T., *Introduction to Optimization*, Optimization Software, New York, 1987
- [12] Reich, S., *Weak convergence theorems for nonexpansive mappings in Banach spaces*, J. Math. Anal. Appl., **67** (1979), 274–276
- [13] Wang, F. and Xu, H. K., *Cyclic algorithms for split feasibility problems in Hilbert spaces*, Nonlinear Anal., **74** (2011), 4105–4111
- [14] Xu, H. K., *Averaged mappings and the gradient-projection algorithm*, J. Optim. Theory Appl., **150** (2011), No. 2, 360–378
- [15] Xu, H. K., *A variable Krasnoselskii-Mann algorithm and the multiple-set split feasibility problem*, Inverse Problems, **22** (2006), 2021–2034

Received: 08.05.2019; In revised form: 16.08.2019; Accepted: 23.08.2019

2010 Mathematics Subject Classification. 90C25, 90C52, 65K10, 47J25.

Key words and phrases. Krasnoselskii-Mann, maximal monotone operator, nonexpansive mapping, cyclic coordinate-update, fixed point algorithm.

Corresponding author: Hong-Kun Xu; xuhk@hdu.edu.cn

DEPARTMENT OF MATHEMATICS
HANGZHOU DIANZI UNIVERSITY
SCHOOL OF SCIENCE
HANGZHOU 310018, CHINA

E-mail address: 161070021@hdu.edu.cn, xuhk@hdu.edu.cn