Dedicated to Prof. Billy E. Rhoades on the occasion of his 90th anniversary

Caristi type fixed point theorems using Száz principle in quasi-metric spaces

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ABSTRACT.

In this paper, we use Száz maximum principle to prove generalizations of Caristi fixed point theorem in a preordered K-complete quasi metric space. Examples are given to support our results.

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