

Dedicated to Prof. Billy E. Rhoades on the occasion of his 90th anniversary

On the geometry of b -distances and the fixed points of mappings

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ABSTRACT.

In the present article we study the geometrical configuration of b -perturbation of the norm of the normed space. The notion of b -metric is important in the solving of the fixed point problem.

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