

New univalence criteria for an integral operator with Mocanu's and Şerb's lemma

CAMELIA BĂRBATU and DANIEL BREAZ

ABSTRACT.

In this paper we consider a general integral operator for analytic functions in the open unit disk \mathbb{U} and we obtain sufficient conditions for univalence of this integral operator, using Mocanu's and Şerb's Lemma. This integral operator was considered in a recent work Bărbatu, C. and Breaz, D., [*The univalence conditions for a general integral operator*, Acta Univ. Apulensis Math. Inform., 57 (2019), 133–145]. The results derived in this paper are shown to follow upon specializing the parameters involved in our results. Several corollaries of the main results are also considered.

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Received: 20.10.2019; In revised form: 04.05.2020; Accepted: 11.05.2020

2010 Mathematics Subject Classification. 30C45, 30C75.

Key words and phrases. *Integral operators, analytic and univalent functions, open unit disk, univalence conditions, Mocanu's and Şerb's Lemma, Schwarz Lemma.*

Corresponding author: Camelia Bărbatu; camipode@yahoo.com

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“BABEŞ-BOLYAI” UNIVERSITY
FACULTY OF MATHEMATICS AND COMPUTER SCIENCES
KOGĂLNICEANU 1, 400084 CLUJ-NAPOCA, ROMANIA

DEPARTMENT OF MATHEMATICS
“1 DECEMBRIE” UNIVERSITY
GABRIEL BETHLEN 5, 510009 ALBA-IULIA, ROMANIA
Email address: camipode@yahoo.com
Email address: dbreaz@uab.ro